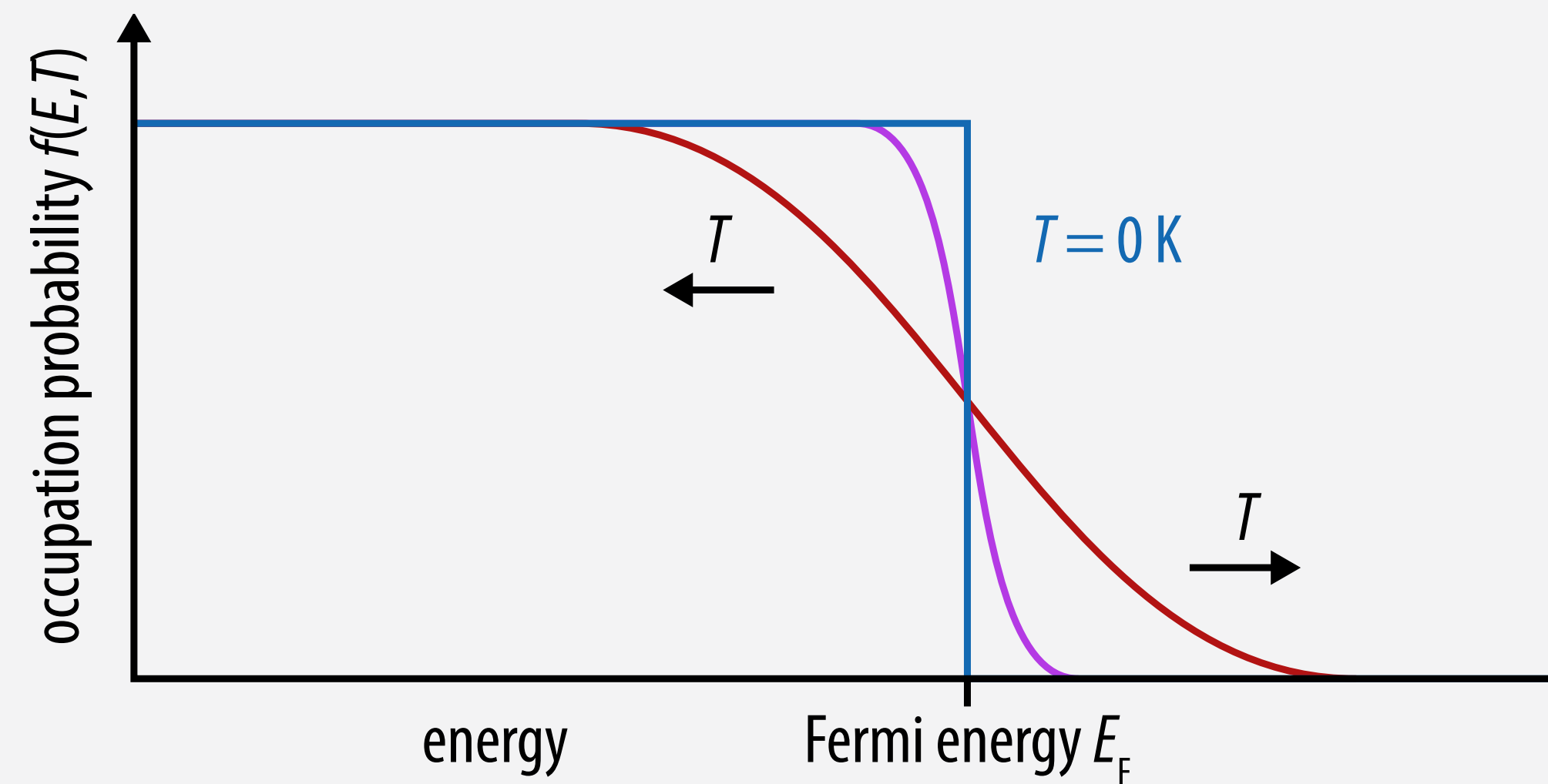


5.4 Charges at Interfaces

Fermi Distribution and Fermi Level

- Fermi-Dirac distribution for thermal distribution of electron energies

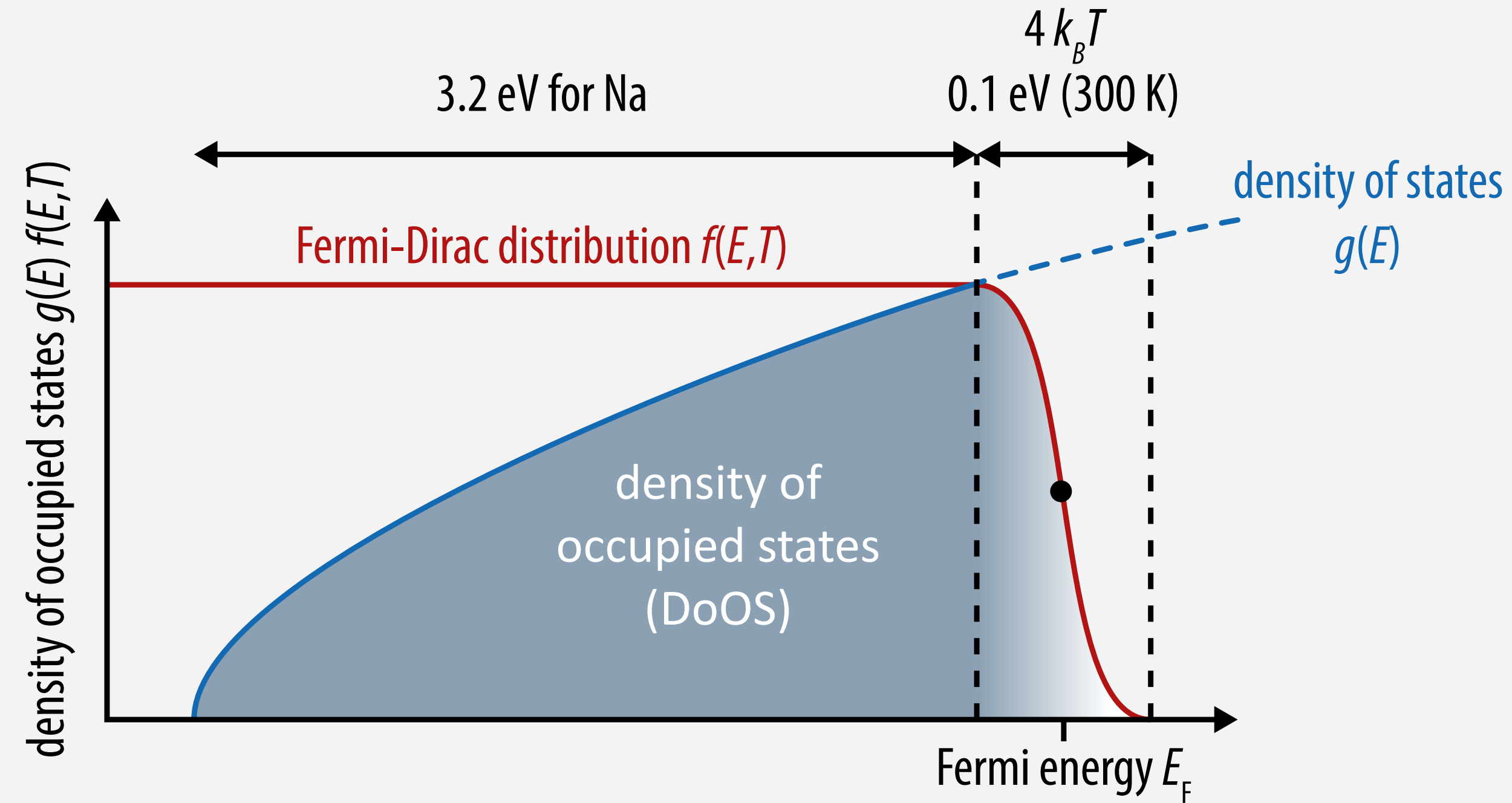
$$f(E) = \frac{1}{e^{\frac{(E - E_F)}{k_B T}} + 1}$$



- for $E - E_F \gg k_B T$, the Fermi-Dirac distribution becomes the Boltzmann distribution
- Fermi energy E_F is **defined** as the energy with the probability to find an electron **$f(E_F) = 0.5$**

Density of Occupied States (DOS)

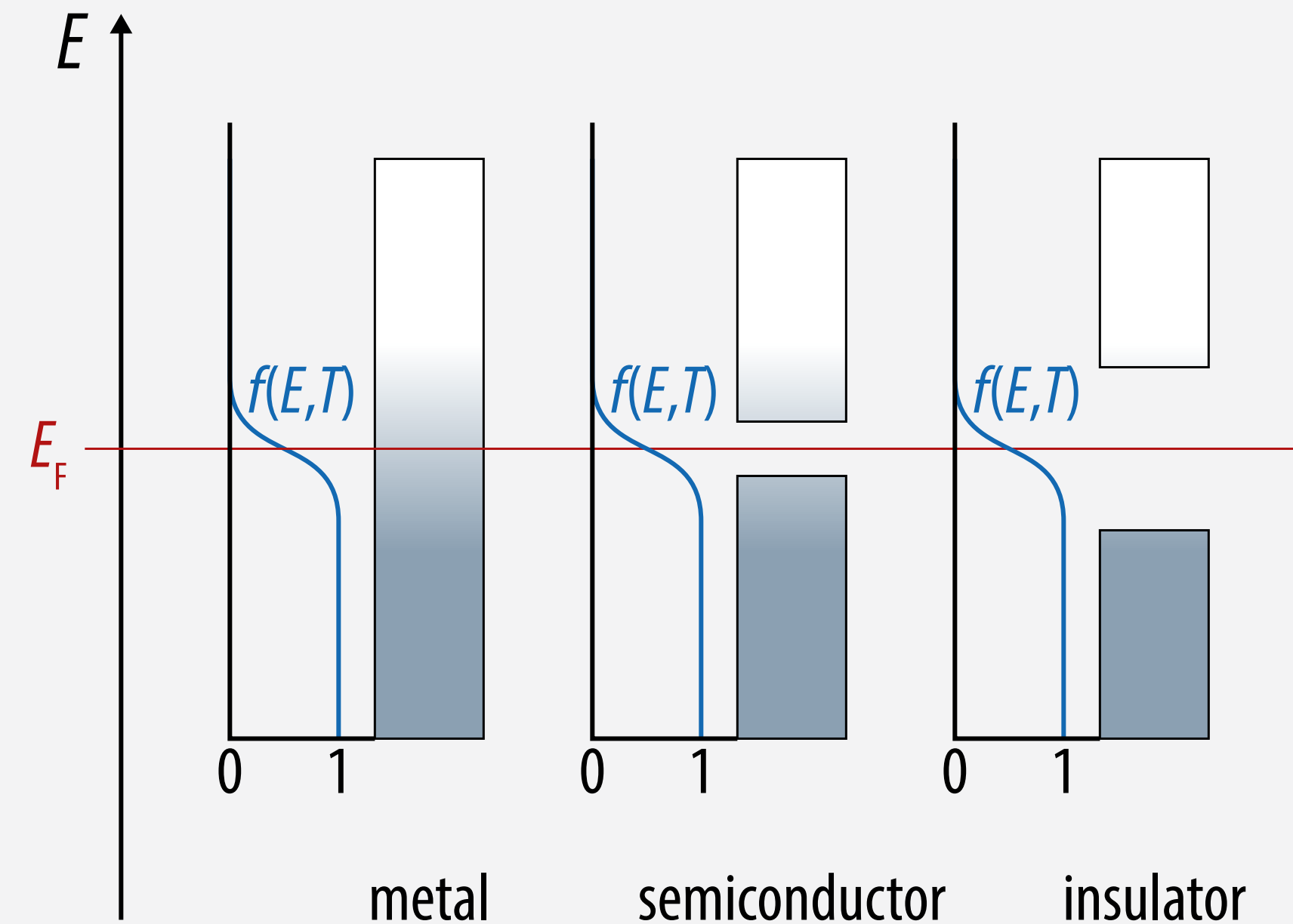
- electronic structure of a material is described by the **density of occupied states (DoOS)**



- **density of states $g(E)$** represents all allowed states of a material (e.g., the 3s band in Na)
- these available states filled according to **Fermi-Dirac distribution $f(E, T)$**
- **density of occupied states $g(E) \cdot f(E, T)$** represents states of all electrons at given temperature

Density of Occupied States in Metals, Semiconductors, Insulators

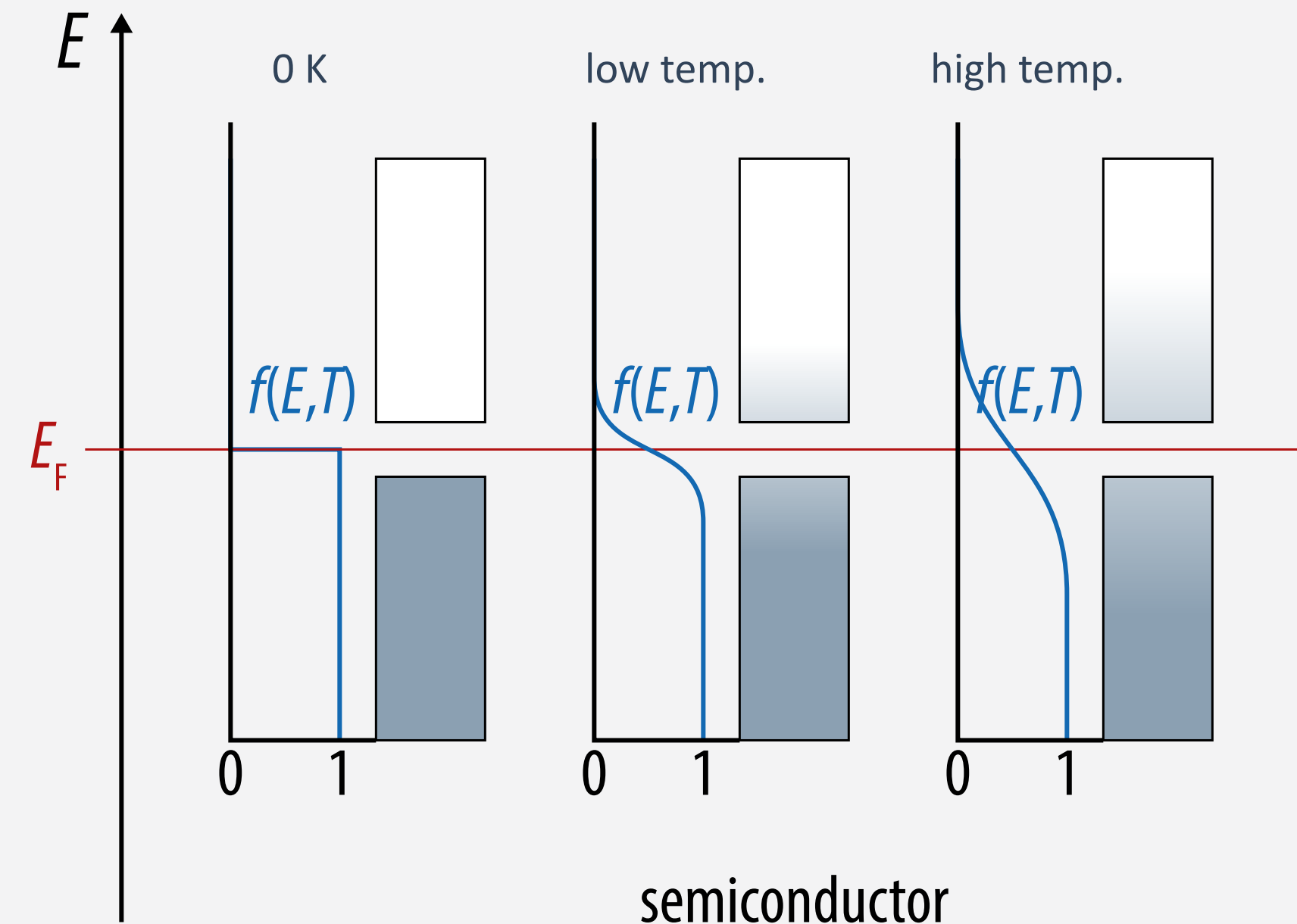
- in metallic conductors, Fermi level is equal to the “work function” (ionization energy) !
- in semiconductors / insulators, the Fermi level is, by definition, in the middle of the bandgap !



- for semiconductors and insulators, density of states within the bandgap $g(E) = 0$
- hence, also density of occupied states is $g(E) \cdot f(E, T) = 0$ within the bandgap
- Fermi level not equal to work function (ionization energy, HOMO level)

Temperature-Dependent Density of Occupied States in Semiconductors

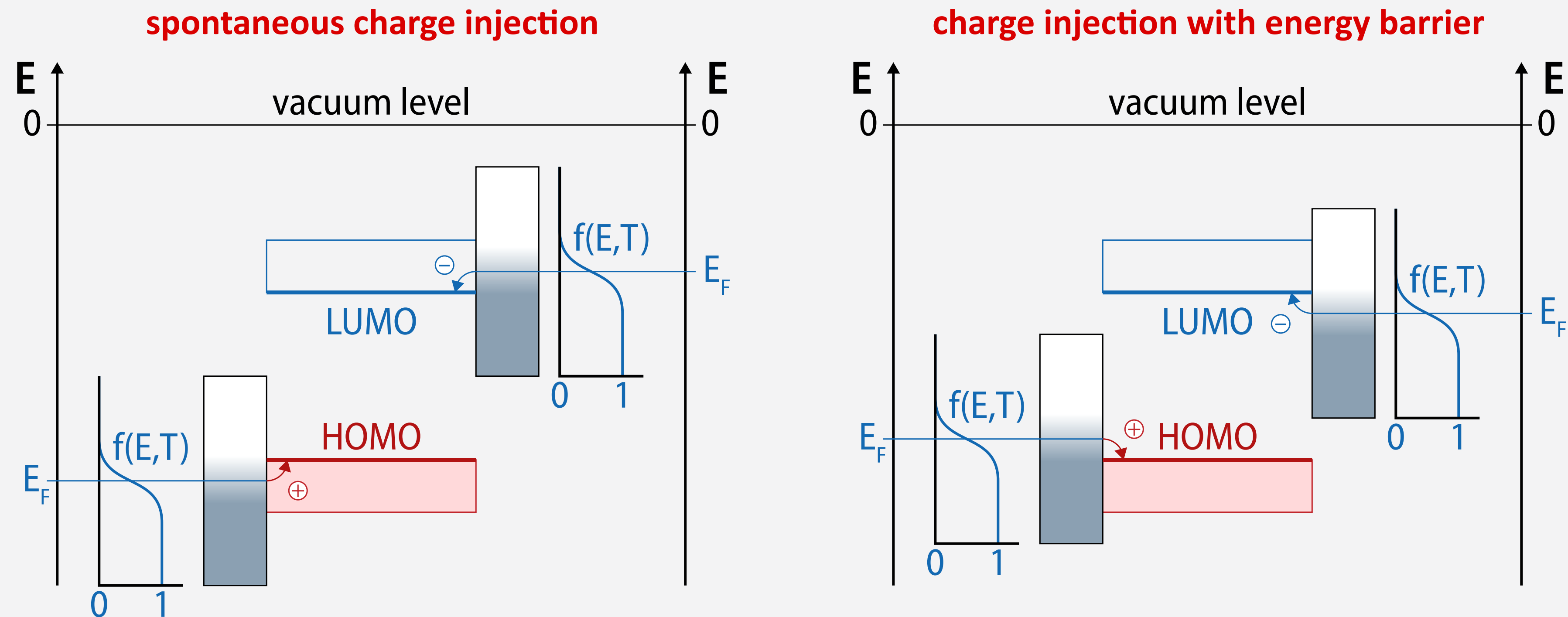
- Fermi distribution of electron energies is temperature-dependent
- a good approximation for “thermal spread” of electron energies is $4 k_B T$



- **only a tiny fraction of “intrinsic” charge carriers in organic semiconductors** (large $E_g \gg 4 k_B T$)
- for silicon (bandgap 1.1 eV): 10^{10} cm^{-3} (10^{-12} at\%) at 300 K, 10^{14} cm^{-3} (10^{-9} at\%) at 500 K

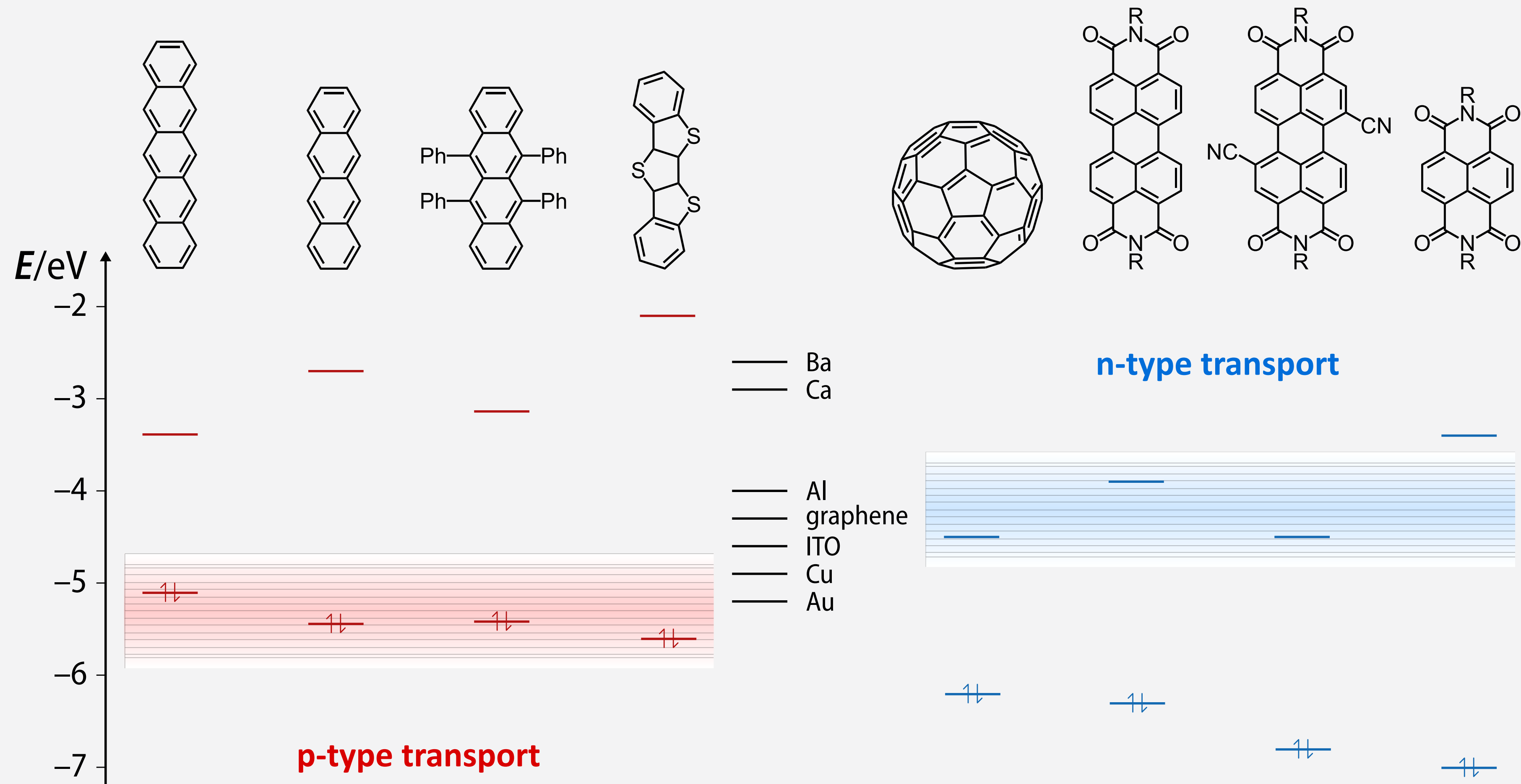
Ideal Metallic Electrodes in Organic Semiconductor Device

- organic semiconductors have low intrinsic charge carrier density and low charge mobility
- like for a metal-insulator contact, all energy levels **pinned at the interface without variation**



- spontaneous electron (hole) injection if HOMO (LUMO) above (below) electrode Fermi level
- otherwise, charge injection with an energy barrier, can be forced in an electric field

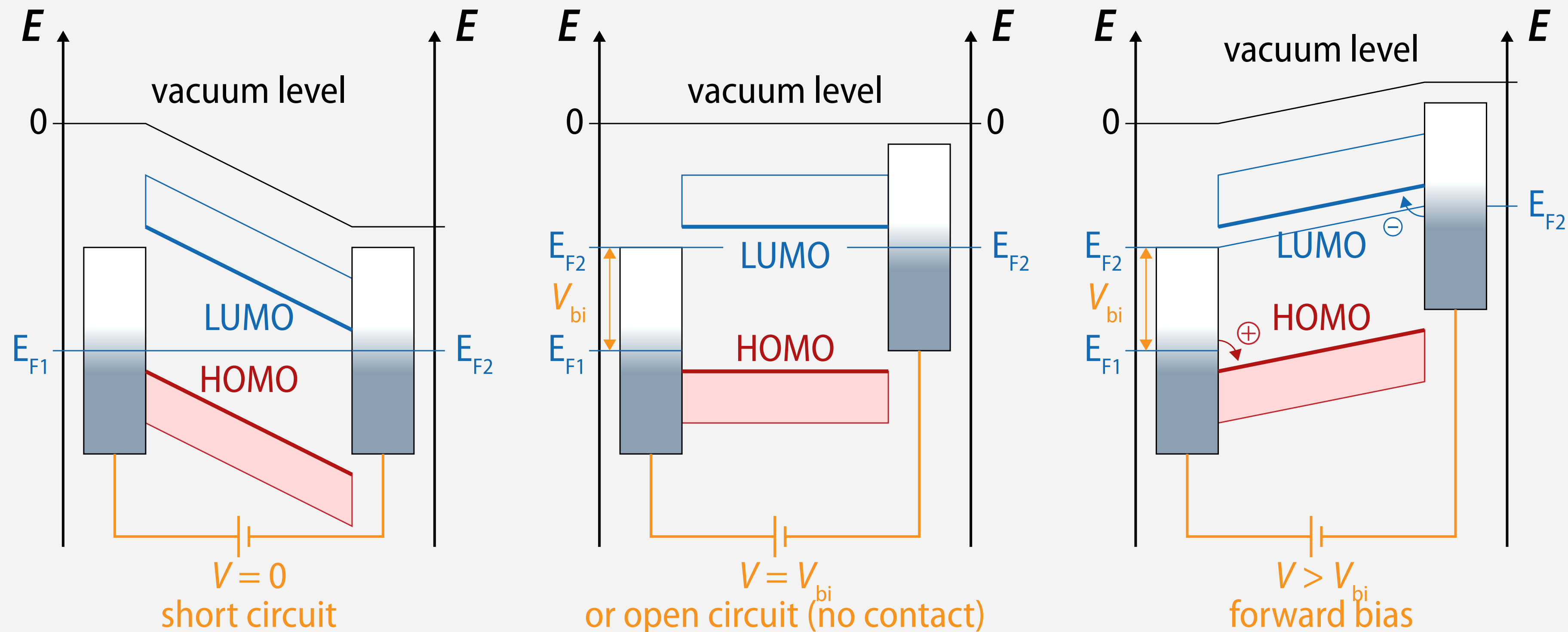
Typical Electrode Materials and Organic Semiconductors



- difficult to find materials with good work functions that are chemically stable & processable
- particularly spontaneous electron injection requires non-noble metals (not air stable)

Materials Interfaces in Electric Contact

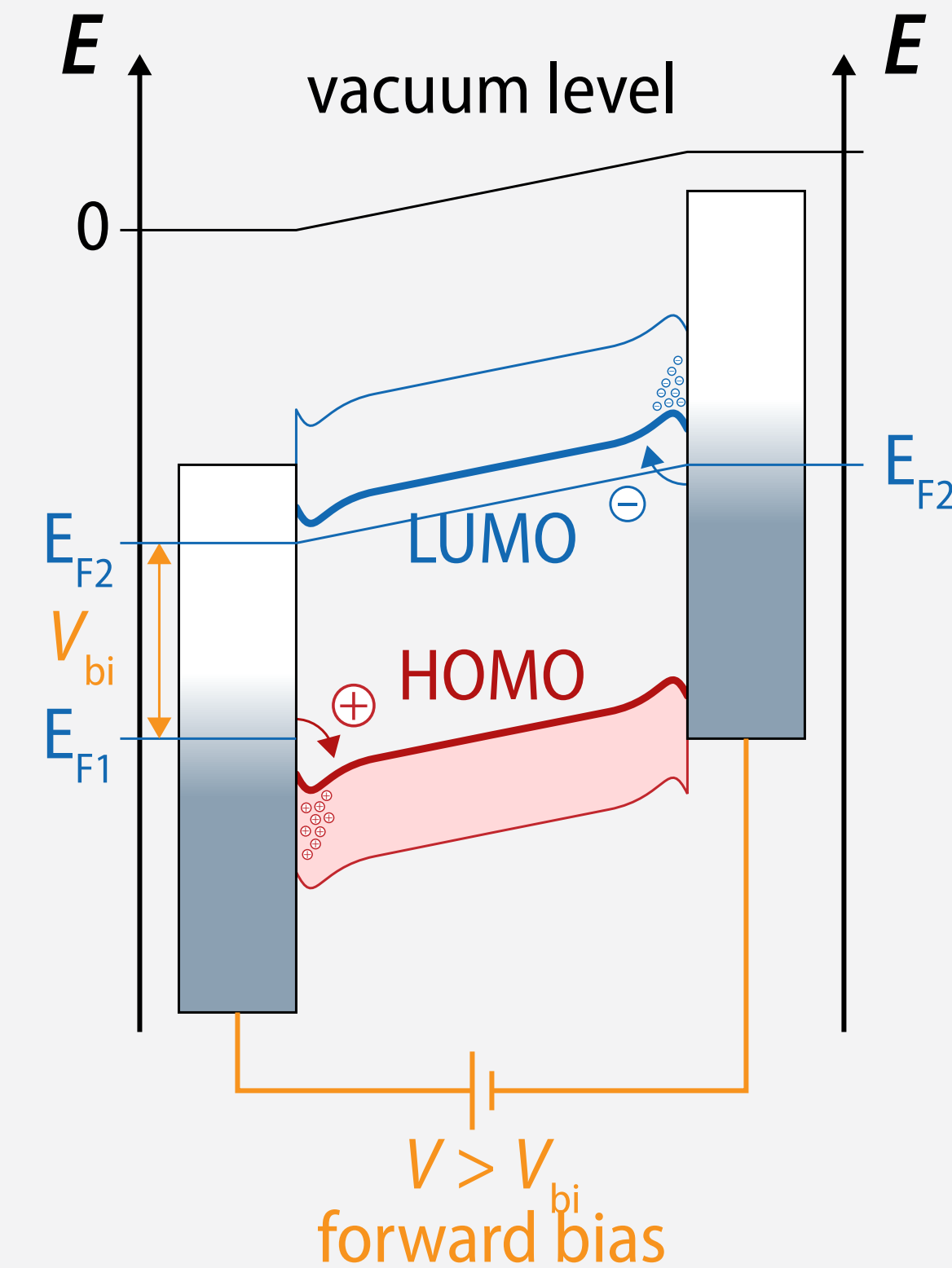
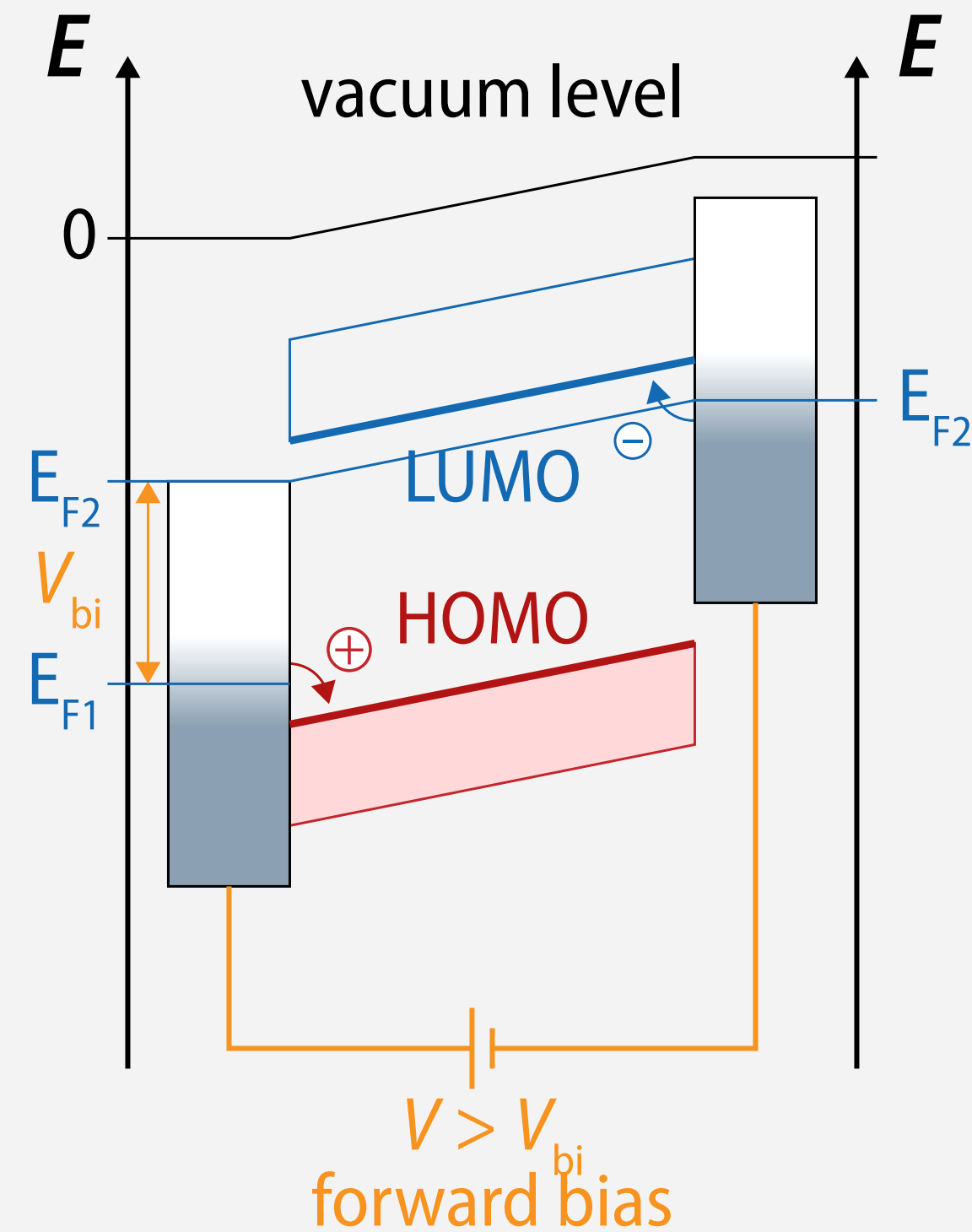
- flat & unaltered HOMO/LUMO levels as long as two (different) electrodes not connected
- built-in potential V_{bi} corresponds to difference in the Fermi levels of the electrodes



- upon external connection, charges flow to equilibrate the Fermi levels of the electrodes
- potential drop across the organic semiconductor layer according to $dU = -e (V_{bi}/x_0) dx$
- **charge injection from the electrodes only possible for forward bias $V > V_{bi}$**

Band Bending

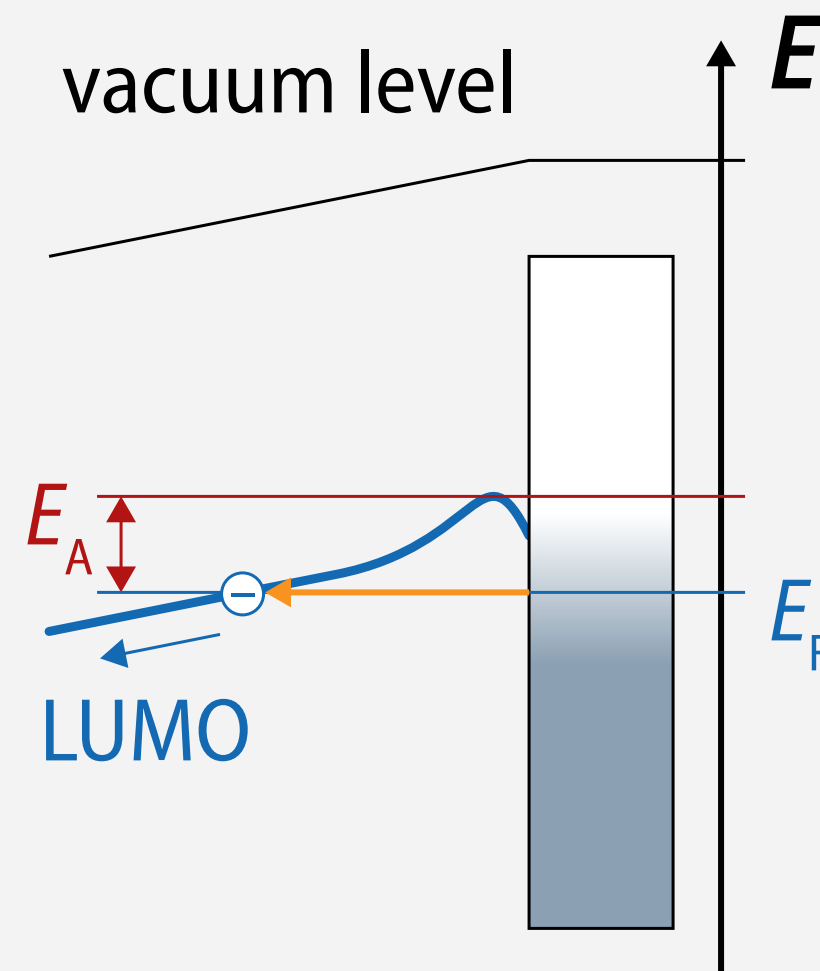
- metal electrodes form “Ohmic contact” with organic semiconductor
- anode (cathode) has an unlimited capacity to inject holes (electrons)



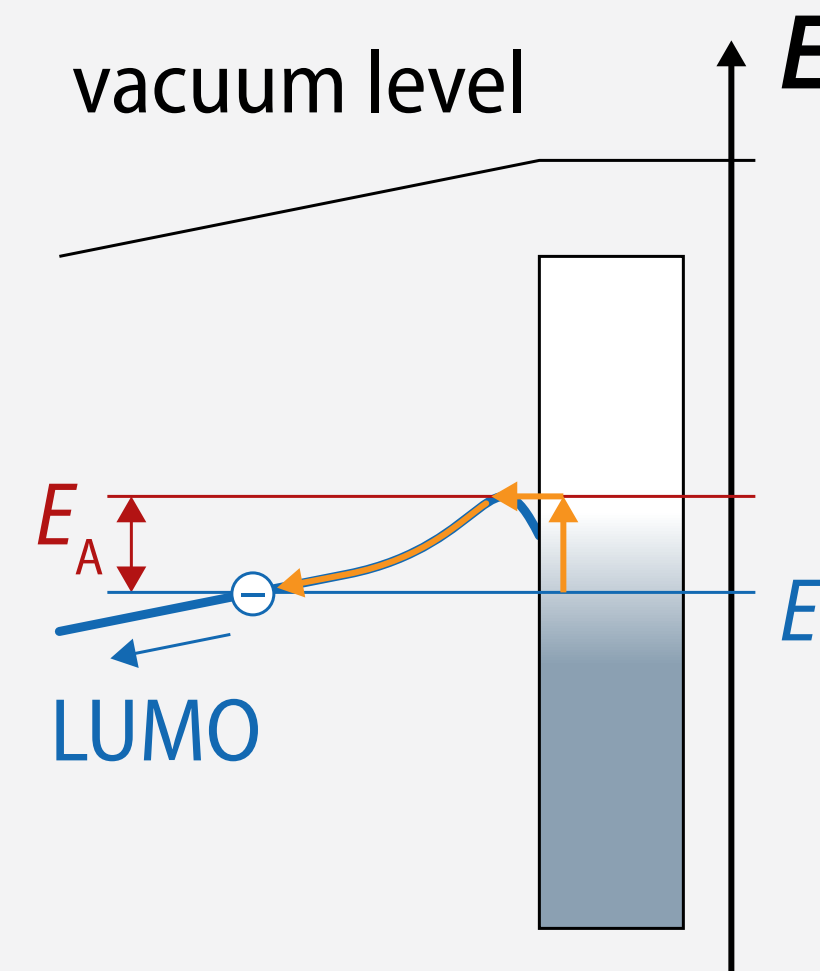
- formation of a “space charge layer” results in additional potential, “band bending”
- layer width $W \propto \epsilon_r^{1/2}$, therefore smaller for organic materials, about 10–30 nm

Band Bending

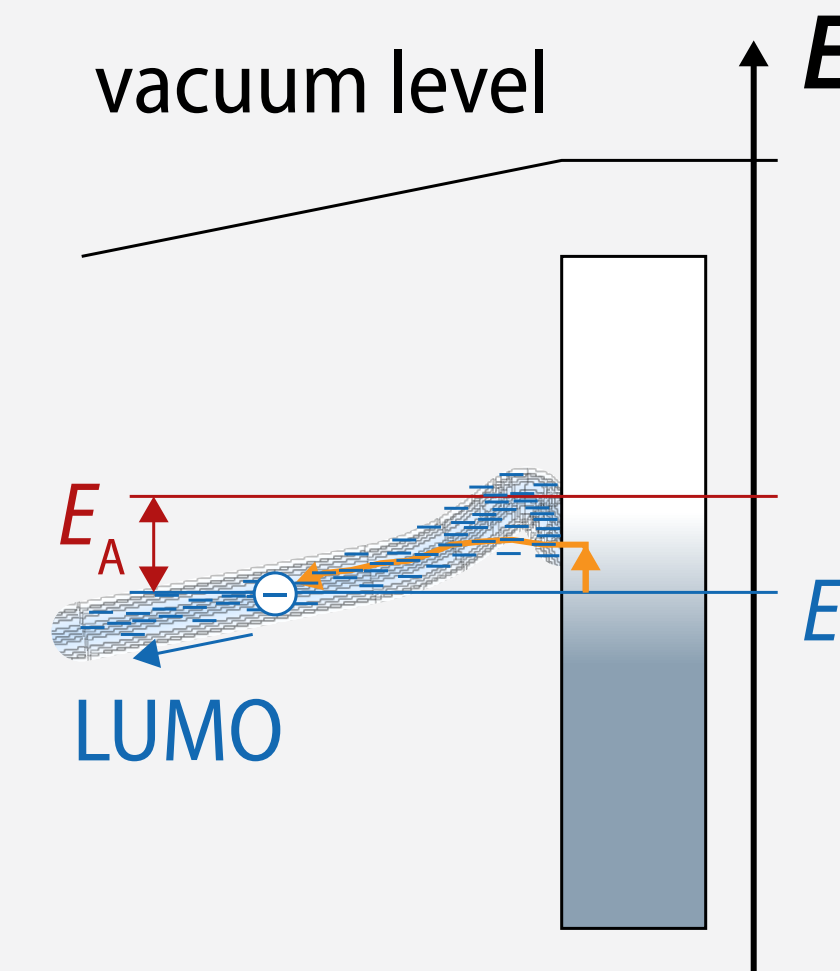
- activation energy barrier E_A for injection due to work function mismatch and band bending



Fowler-Nordheim
tunneling



Richardson-Schottky
thermionic injection



hopping injection into
disordered semiconductor

- **tunneling:** at high applied electric field electrons can quantum-mechanically tunnel through the narrow (5–10 nm) triangular barrier
- **thermionic emission:** electrons are thermally excited above the activation barrier and diffuse out of the interface
- **hopping:** in a disordered material, the energy distribution of localized states offers pathways with lower thermal activation via “trap states”

Learning Outcome

- **metal electrodes in contact with organic semiconductor**
 - work function of the metal should be close to active transport region
 - high work function (noble metals) for hole injection/extraction
 - low work function metals for electron injection/extraction
 - Ohmic “metal-insulator”-type contact results in space charge layer and band bending
- **energy barrier for charge injection due to work function mismatch and band bending**
 - energy barrier can be overcome in case of a “forward bias” electric field
 - injection possible via tunneling, thermionic injection, or hopping
 - injection most commonly occurs by hopping, making use of “trap states”

